

## Spheres Surface Area and Volume Worksheet

- 1) A sphere has a radius of 8 cm. Find its volume and surface area.  
Give your answers to 3 significant figures. Use  $\pi = 3.142$

$$S = 4\pi r^2 = 4\pi(8)^2 = 256\pi \approx 804.248 \text{ cm}^2$$

$$V = \frac{4}{3}\pi r^3 = \frac{4}{3}\pi(8)^3 \approx 2144.661 \text{ cm}^3$$

- 2) A hemispherical bowl has a radius of 15 cm. It is filled completely with water and covered with a lid.

(a) Find the volume of the water.

(b) Find the surface area of the bowl (including the lid).

Give your answers to 3 significant figures. Use  $\pi = 3.142$

$$a) V = \frac{1}{2} \cdot \frac{4}{3}\pi r^3 = \frac{2}{3}\pi(15)^3 \approx 7068.583 \text{ cm}^3$$

$$b) S = 3\pi r^2 = 3\pi(15)^2 \approx 2120.575 \text{ cm}^2$$

- 3) A bowl has the form of a hollow hemisphere with a radius of 8.4 cm.  
Find the external surface area and the volume of the bowl.  
Give your answers to 3 significant figures. Use  $\pi = 3.142$

$$S = \frac{1}{2} \cdot 4\pi r^2 = 2\pi(8.4)^2 \approx 443.342 \text{ cm}^2$$

$$V = \frac{1}{2} \cdot \frac{4}{3}\pi r^3 = \frac{2}{3}\pi(8.4)^3 \approx 1241.356 \text{ cm}^3$$

- 4) Find the surface area of a sphere whose volume is  $288\pi \text{ cm}^3$ .  
Give your answer to 3 significant figures. Use  $\pi = 3.142$

$$V = \frac{4}{3}\pi r^3$$

$$288\pi = \frac{4}{3}\pi r^3$$

$$216 = r^3$$

$$r = 6$$

$$\rightarrow S = 4\pi r^2 = 4\pi(6)^2 \approx 452.389 \text{ cm}^2$$

- 5) Find the volume of an open hemisphere whose external surface area is  $1762 \text{ cm}^2$ .  
Give your answer to 3 significant figures. Use  $\pi = 3.142$

$$S = \frac{1}{2} \cdot 4\pi r^2$$

$$1762 = 2\pi r^2$$

$$280.431 \approx r^2$$

$$16.746 \approx r$$

$$V = \frac{1}{2} \cdot \frac{4}{3} \pi r^3 = \frac{2}{3} \pi (16.746)^3 \approx 9835.528 \text{ cm}^3$$

- 6) The surface area of a closed hemisphere is given as  $618 \text{ cm}^2$ .

- (a) Find the radius of the hemisphere.  
(b) Find the volume of the hemisphere.  
(c) Find the external surface area of the hemisphere if it were hollow.

Give your answers to 3 significant figures. Use  $\pi = 3.142$

$$a) S = 3\pi r^2$$

$$618 = 3\pi r^2$$

$$65.572 \approx r^2$$

$$8.098 \approx r$$

$$b) V = \frac{1}{2} \cdot \frac{4}{3} \pi r^3 = \frac{2}{3} \pi (8.098)^3 \approx 1112.076 \text{ cm}^3$$

$$c) S = \frac{1}{2} \cdot 4\pi r^2 = 2\pi (8.098)^2 \approx 412 \text{ cm}^2$$

OR

$$S = \frac{2}{3} \cdot 618 = 412$$

- 7) A hemispherical bowl has a radius of  $10 \text{ cm}$ .

- (a) Find the volume of the bowl.  
(b) Find the external surface area of the bowl.  
(c) A cylinder of radius  $7 \text{ cm}$  and height  $h \text{ cm}$  has the same volume as the bowl. Calculate the value of  $h$ .

Give your answers to 3 significant figures. Use  $\pi = 3.142$

$$a) V = \frac{1}{2} \cdot \frac{4}{3} \pi r^3 = \frac{2}{3} \pi (10)^3 \approx 2094.395 \text{ cm}^3$$

$$b) S = \frac{1}{2} \cdot 4\pi r^2 = 2\pi (10)^2 \approx 628.319 \text{ cm}^2$$

$$c) V_{\text{cyl}} = \pi r^2 h$$

$$2094.395 = \pi (7)^2 h$$

$$h \approx 13.605 \text{ cm}$$