# Geometry Info Sheet \#16 

New Theorems; Example Geometric Proofs

## Theorems

Congruent Supplements Theorem:
If two angles are supplements of congruent angles (or of the same angle), then the two angles are congruent.

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## Example Proofs

Given: $\angle 1 \cong \angle 3$
$\angle 1$ and $\angle 2$ are supplementary
$\angle 3$ and $\angle 4$ are supplementary
Prove: $\angle 2 \cong \angle 4$ (Congruent Supplements Theorem)

| Step \# | Statement | Reason |
| :---: | :---: | :---: |
| 1. | $\angle 1 \cong \angle 3$ | Given |
| 2. | $\mathrm{m} x 1=\mathrm{m}$ ¢ 3 | Two congruent angles have equal measures |
| 3. | $\angle 1$ and $\angle 2$ are supplementary | Given |
| 4. | $\angle 3$ and $\angle 4$ are supplementary | Given |
| 5. | $\mathrm{m} \Varangle 1+\mathrm{m} \Varangle 2=180^{\circ}$ | Definition of Supplementary Angles |
| 6. | $\mathrm{m} \Varangle 3+\mathrm{m} \Varangle 4=180^{\circ}$ | Definition of Supplementary Angles |
| 7. | $m \nless 1+m \nless 2=m \Varangle 3+m \nless 4$ | Substitution Property of Equality (from steps 5 and 6) |
| 8. | $m \not m 1+m \nless 2=m \Varangle 1+m \nless 4$ | Substitution Property of Equality (from steps 2 and 7) |
| 9. | $\mathrm{m} \Varangle 2=\mathrm{m}$ ¢ 4 | Subtraction Property of Equality |
| 10. | $\angle 2 \cong \angle 4$ | Two angles with equal measures are congruent |

Given: $\angle 1$ and $\angle 2$ are supplementary $\angle 1$ and $\angle 3$ are supplementary

Prove: $\angle 2 \cong \angle 3$ (Congruent Supplements Theorem)


| Step \# | Statement | Reason |
| :---: | :--- | :--- |
| 1. | $\angle 1$ and $\angle 2$ are supplementary <br> $\angle 1$ and $\angle 3$ are supplementary | Given |
| 2. | $m \Varangle 1+m \Varangle 2=180^{\circ}$ <br> $m \Varangle 1+m \Varangle 3=180^{\circ}$ | Definition of Supplementary Angles |
| 3. | $m \Varangle 1+m \Varangle 2=m \Varangle 1+m \Varangle 3$ | Substitution Property of Equality (from step 2) |
| 4. | $m \Varangle 1=m \Varangle 1$ | Reflexive Property of Congruence This step can be skipped. |
| 5. | $m \Varangle 2=m \Varangle 3$ | Subtraction Property of Equality |
| 6. | $\angle 2 \cong \angle 3$ | Two angles with equal measures are congruent |

